



# On the Unification of the Constants of Nature

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A short essay that unifies gravity and electromagnetism with a system of natural units that are based upon a Helium nucleus (Alpha particle). Alternative definitions for Planck's constant and the fine structure constant are deduced and the standard gravitational parameter of a Helium nucleus is shown to be directly proportional to the square of its electromagnetic frequency.

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## INTRODUCTION

The magnetic flux quantum  $\Phi_0$  is equivalent to<sup>[1], [2], [3]</sup>

$$(1) \quad \Phi_0 = \frac{h}{Z_0},$$

where  $h$  is Planck's constant<sup>[4]</sup> and  $Z_0$  is the charge of an alpha particle ( $2e$ ). Planck's reduced constant  $\hbar$  is

$$(2) \quad \hbar = \frac{h}{2\pi},$$

which can also be defined with Bohr's radius  $r_B$  as

$$(3) \quad \hbar = \alpha m_e r_B c,$$

where  $\alpha$  is the fine structure constant,  $m_e$  is the mass of a Beta particle, and  $c$  is the speed of light in a vacuum. Combining Eqs. (1) through (3) yields

$$(4) \quad 2\pi\hbar^2 = Z_0\Phi_0\alpha m_e r_B c, \text{ or } h = \sqrt{Z_0\Phi_0\alpha m_e 2\pi r_B c}.$$

Bohr, however, did not deduce his radius  $r_B$  from an Alpha particle ( $Z_0 = 2e =$  a Helium nucleus and not a Hydrogen nucleus). The adjusted radius  $r_0$  for a Helium atom can be deduced from Eq. (4) as  $r_0 \approx 0.529177211 \times 10^{-10}$  m.

## WAVE-PARTICLE DUALITY AND A NEW DEFINITION FOR THE FINE STRUCTURE CONSTANT

A particle's wavelength  $\lambda$  can be determined with de Broglie's matter wave equation

$$(5) \quad \lambda = \frac{h}{p} = \frac{2\pi\hbar}{mv},$$

where  $p$  is the particle's momentum and  $v$  is its speed. With the mass quantized in units of  $m_e$ , a Beta particle's ground state wavelength relative to the electric and magnetic flux quanta of a Helium nucleus can be deduced from Eqs. (4) & (5) as

$$(6) \quad \lambda_0 = \frac{2\pi\hbar}{m_e v_0} = \frac{Z_0 \Phi_0 \alpha r_0 c}{\hbar v_0}.$$

The Beta particle's ground state frequency  $f_0$  is then

$$(7) \quad f_0 = \frac{v_0}{\lambda_0} = \frac{\hbar v_0^2}{Z_0 \Phi_0 \alpha r_0 c},$$

and a wave mechanical definition for the fine structure constant can be given as

$$(8) \quad \alpha = \frac{\hbar \lambda_0 v_0}{Z_0 \Phi_0 r_0 c} = \frac{\lambda_0 v_0}{2\pi r_0 c}.$$

Eq. (8) suggests  $v_0 \approx \alpha c$ . The energy of electromagnetic radiation ( $E = hf$ ) is simply the product of the electric, magnetic, and frequency quanta;

$$(9) \quad E = Z_0 \Phi_0 f_0.$$

## CONCLUSION

The Gaussian gravitational constant  $k_0$  (not to be confused with the Coulomb constant  $k_e$ ) is

$$(10) \quad k_0 = \sqrt{G} = \frac{2\pi}{T\sqrt{M_1 + M_2}},$$

where  $G$  is Newton's gravitational constant,  $T$  is the orbital period, and  $M_1$  and  $M_2$  are the masses of the system. Setting the total mass of the system to the mass of an Alpha particle  $M_A$  ( $M_A = 2M_P + 2M_N$  where  $M_P$  and  $M_N$  are the proton and neutron masses), the quantized relationship between the Gaussian gravitational constant  $k_0$  and the electromagnetic frequency of an Alpha particle can be given as

$$(11) \quad k_0 = \frac{2\pi f_0}{\sqrt{M_A}}, \quad 2\pi = \frac{Z_0 \Phi_0}{\hbar}, \quad k_0 = \frac{Z_0 \Phi_0 f_0}{\hbar \sqrt{M_A}} = \frac{E}{\hbar \sqrt{M_A}}.$$

The standard gravitational parameter  $\mu$  for the Alpha particle is therefore

$$(12) \quad GM_A = \mu = \left(\frac{E}{\hbar}\right)^2,$$

and the energy of its electromagnetic frequency is

$$(13) \quad E = \hbar \sqrt{\mu}.$$

Could Eq. (13) help explain dark energy? The nuclear frequency  $f_n$  of an atom would then be

$$(14) \quad f_n = \frac{\sqrt{\mu n}}{2\pi},$$

where  $n$  is the nuclear mass number relative to a Helium nucleus. For Hydrogen,  $n = 1/2$ , Helium,  $n = 1$ , Lithium,  $n = 1\frac{1}{2}$ , Beryllium,  $n = 2$ , etcetera.

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